

NGC 1261: A TIME-SERIES VI STUDY OF ITS VARIABLE STARS

A. Arellano Ferro¹, I. H. Bustos Fierro², J. H. Calderón^{2,3}, and J. A. Ahumada²

Received June 1 2019; accepted August 13 2019

ABSTRACT

Time-series VI CCD photometry of the globular cluster NGC 1261 is employed to study its variable star population. A membership analysis of most variables based on Gaia DR2 proper motions and colours was performed prior to the estimation of the mean cluster distance and metallicity. The light curves of the member RR Lyrae were Fourier decomposed to calculate their individual values of distance, [Fe/H], radius and mass. The *I*-band P-L for RR Lyrae stars was also employed. Our best estimates of the metallicity and distance of this Oo I cluster are $[\text{Fe}/\text{H}]_{\text{ZW}} = -1.42 \pm 0.05$ dex and $d = 17.2 \pm 0.4$ kpc. No mixture of fundamental and first overtone RR Lyrae stars in the either-or or bimodal region is seen in this cluster, as it seems to be the rule for Oo I clusters with a red horizontal branch. A multi-approach search in a region of about $10' \times 10'$ around the cluster revealed no new variable stars within the limitations of our CCD photometry.

RESUMEN

Empleamos una serie temporal de imágenes CCD en las bandas VI del cúmulo globular NGC 1261, para estudiar su población de estrellas variables. Se realizó un análisis de la membresía de las estrellas variables basado en movimientos propios y colores dados en Gaia DR2. Por medio de la descomposición de Fourier de curvas de luz de estrellas RR Lyrae, se obtuvieron sus valores individuales de distancia, [Fe/H], radio y masa. También utilizamos la relación P-L en la banda *I* para las RR Lyrae. Nuestras estimaciones de la metalicidad y la distancia medias de NGC 1261, un cúmulo de tipo Oo I, son $[\text{Fe}/\text{H}]_{\text{ZW}} = -1.48 \pm 0.05$ dex y $d = 17.2 \pm 0.4$ kpc. No se observa mezcla de modos de pulsación fundamental y primer sobretono de RR Lyrae en la región bimodal, como parece ser la norma para cúmulos de tipo OoI con rama horizontal roja. Una búsqueda cuidadosa en la región de $10' \times 10'$ centrada en el cúmulo no reveló nuevas variables, dentro de las limitaciones de nuestra fotometría.

Key Words: globular clusters: individual: NGC 1261 — stars: variables: RR Lyrae — stars: fundamental parameters

1. INTRODUCTION

The southern globular cluster NGC 1261 (C0310–554), also known as Caldwell 87, is located in the constellation Horologium ($\alpha = 03^{\text{h}}12^{\text{m}}16.21^{\text{s}}$, $\delta = -55^{\circ}12'58.4''$, J2000, Goldsbury et al. (2010)). It was discovered by James Dunlop in 1826, and remained little studied until the mid-XXth century. It is a cluster of intermediate brightness, located far from the bulge of the Galaxy ($l = 270.54^{\circ}$,

$b = -52.12^{\circ}$) and, consequently, has negligible or no reddening. The Catalog of Parameters for Milky Way Globular Clusters compiled by Harris (1996) (2010 edition), lists a metallicity $[\text{Fe}/\text{H}] = -1.27$, a distance to the Sun of 16.4 kpc, the level of the Horizontal Branch (HB) as $V_{\text{HB}} = 16.7$ mag, and a reddening $E(B - V) = 0.01$. The Catalogue of Variable Stars in Globular Clusters (CVSGC), (Clement et al. 2001) (2017 edition), lists 31 stars, although only 29 have been confirmed as variables: RR Lyrae stars (23), SX Phe (3), variable red giants or SR (2) and eclipsing binaries EC? (1). The members of the RR Lyrae population were first reported from photographic studies by Laborde & Fourcade (1966), later on by Bartolini et al. (1971), Wehlau & Demers

¹Instituto de Astronomía, Universidad Nacional Autónoma de México, México.

²Universidad Nacional de Córdoba, Observatorio Astronómico, Córdoba, Argentina.

³Consejo Nacional de Investigaciones Científicas y Técnicas (CONICET), Buenos Aires, Argentina.

(1977), Wehlau et al. (1977) and, more recently, in the CCD studies of Salinas et al. (2007) and Salinas et al. (2016), who discovered five RR Lyrae stars, three SX Phoenicis, one long period variable and an eclipsing binary of the W UMa type.

So far, the variable star population of NGC 1261 has not been studied with the specific aim of estimating some of the physical properties of the cluster, such as the mean metallicity, distance and age, by performing a detailed analysis of the light curves. Likewise, the distribution of variables in the HB has not been discussed along with an analysis of individual membership. Studies of the distribution of RR Lyrae pulsation modes in the instability strip around the first overtone red edge (FORE), have shown that the modes are neatly split in all Oo II clusters with blue HB's; however, this happens only in some of the Oo I Type clusters with redder HB's (e. g. Arellano Ferro et al. (2018b)). It has been argued that this property is related to the distribution of stars in the zero-age horizontal branch (ZAHB) which, in turn, depends on the mass loss during the He-flashes at the asymptotic giant branch (AGB) (Arellano Ferro et al. 2018a; Caputo et al. 1978). The facts that NGC 1261 is among the few Oo I clusters with extremely red HB, has intermediate metallicity and harbours numerous RR Lyrae stars of both modes, add a particular interest to its study.

In the present work we perform such an analysis based on a new, extensive time-series of *VI* CCD images. The specific calibrations for different families of variable stars, concerning Fourier light curve decomposition, luminosity of the horizontal branch, and P-L relations are discussed. We also make use of the possibility of ensuring the membership of the variables to the cluster through the analysis of proper motions available in the Gaia DR2 catalogue. The paper is structured in the following way: In § 2, we describe our observations, the data reduction process and the transformation to the standard photometric system. In § 3, we report the periods, epochs and display the *VI* light curves of all variables detected in our photometry. We also discuss the cluster membership and some cases of clear light contamination by extremely close neighbours, as well as the corresponding corrections in amplitude and position, in the colour-magnitude diagram (CMD). Our failed efforts to find new variables are described. In § 4, we present the log *P*-amplitude diagram (Bailey's diagram) to confirm the Oo I type nature of NGC 1261. § 5 describes our estimation of the interstellar reddening. § 6, § 7 and § 8 contain the light curve Fourier decomposition and physical parameters esti-

TABLE 1
THE TIME DISTRIBUTION OF *VI*
OBSERVATIONS OF NGC 1261

Date (y/m/d)	N_V	t_V (s)	N_I	t_I (s)	Avg. seeing (")
2017/08/19	17	400	20	200	3.0
2017/08/20	19	400	25	200	2.9
2017/09/10	15	400	17	200	3.1
2017/09/15	15	400	15	200	3.0
2017/09/22	24	400	29	200	2.3
2017/10/06	15	400	19	200	3.0
2017/10/28	26	400	30	200	3.1
2017/12/07	13	400	14	200	2.4
2018/08/03	4	300	6	150-200	2.9
2018/08/04	27	300	33	150	3.4
2018/08/05	27	300	27	150	2.9
2018/08/11	–	–	23	150	3.0
2018/09/02	33	300	37	150	2.4
2018/09/14	28	300	38	150	2.3
2018/09/16	23	300	29	150	2.3
2018/11/16	18	300	21	150	2.9
2018/11/30	4	300	5	150	2.6
2018/12/16	22	300	24	150	2.5
Total:	330	–	412	–	–

Columns N_V and N_I give the number of images taken with the *V* and *I* filters respectively. Columns t_V and t_I provide the exposure time, or range of exposure times employed during each night for each filter. The average seeing is listed in the last column.

mations, and the comparison with previous determinations of [Fe/H] and distance. In § 9 we comment on the structure of the HB and the correlation with the distribution of RR Lyrae pulsation modes in the instability strip. In § 10 we summarize our work.

2. DATA, OBSERVATIONS AND REDUCTIONS

The data used for the present work were obtained with the 1.54-meter telescope at the Bosque Alegre Astrophysical Station of the Cordoba Observatory, (National University of Cordoba), Argentina, during seventeen nights between August 19th 2017 and November 30th 2018. A total of 330 and 412 *V* and *I* CCD images were acquired. The detector used was a CCD Alta F16M of 4096×4096 square 9-micron pixels, binned 2 × 2, with a scale of 0.496 arcsec/pix (after binning). The images were trimmed to 1200 × 1200 pixels, for a useful field of view (FoV) of approximately 10 × 10 arcmin².

Table 1 summarizes the observation dates, exposure times and average seeing conditions.

2.1. Difference Image Analysis

For the reduction of our data, we employed the software Difference Imaging Analysis (DIA) with its pipeline implementation DanDIA⁴ (Bramich 2008;

⁴DanDIA is built from the DanIDL library of IDL routines available at <http://www.danidl.co.uk>

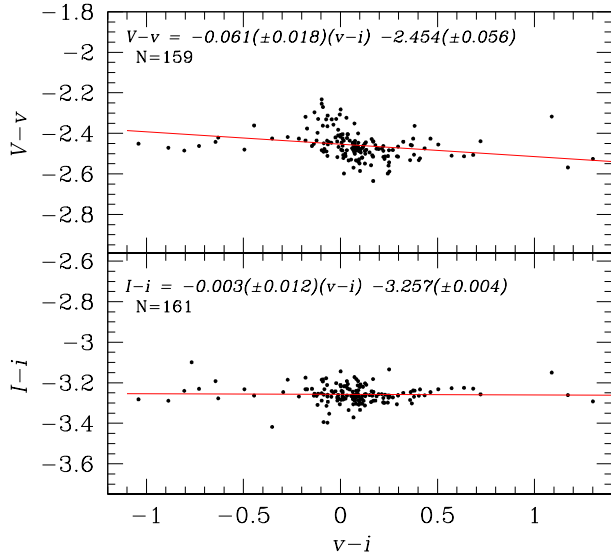


Fig. 1. Transformation relations obtained for the V and I filters between the instrumental and the standard photometric systems. We employed a set of standard stars in the field of NGC 1261 from the collection of Stetson (2000). The colour figure can be viewed online.

Bramich et al. 2013). With this, we were able to obtain high-precision photometry for all the point sources in the FoV of our CCD images. First, a reference image is created by DanDIA by stacking the best images in each filter; then, the reference image is subtracted from the rest of the images. In each reference image, we measured the fluxes (referred to as reference fluxes) and positions of all PSF-like objects (stars) by extracting a spatially variable empirical PSF. This PSF is built from about 300-400 isolated stars, and a third degree polynomial is fitted to each detected object.

Differential fluxes are converted into total fluxes. The total flux $f_{\text{tot}}(t)$ in ADU/s at each epoch t can be estimated as:

$$f_{\text{tot}}(t) = f_{\text{ref}} + \frac{f_{\text{diff}}(t)}{p(t)}, \quad (1)$$

where f_{ref} is the reference flux (ADU/s), $f_{\text{diff}}(t)$ is the differential flux (ADU/s) and $p(t)$ is the photometric scale factor (the integral of the kernel solution). Conversion to instrumental magnitudes was achieved using:

$$m_{\text{ins}}(t) = 25.0 - 2.5 \log [f_{\text{tot}}(t)], \quad (2)$$

where $m_{\text{ins}}(t)$ is the instrumental magnitude of the star at time t . The above procedure has been described in detail in Bramich et al. (2011).

2.2. Photometric Calibrations

2.2.1. Relative Calibration

To correct for possible systematic errors, we applied the methodology developed in Bramich & Freudling (2012) to solve for the magnitude offsets Z_k that should be applied to each photometric measurement from the image k . In terms of DIA, this translates into a correction for the systematic error introduced into the photometry due to a possible error in the flux-magnitude conversion factor (Bramich et al. 2015). In the present case the corrections were very small, ≈ 0.001 mag for stars brighter than $V \approx 18.0$.

2.2.2. Absolute Calibration

Standard stars in the field of NGC 1261 are included in the online collection of Stetson (2000)⁵ and we used them to transform instrumental vi magnitudes into the Johnson-Kron-Cousins standard VI system. These stars are distributed in the cluster periphery, they are generally isolated and can be accurately measured by DanDIA. The mild colour dependence of the standard minus instrumental magnitudes is shown in Figure 1. The transformation equations are explicitly given in the figure itself.

2.2.3. Internal Errors

The internal errors of our CCD photometry can be evaluated via the rms diagram of Figure 2.

3. VARIABLE STARS IN NGC 1261

There are 29 variable stars listed in the Catalogue of Variable Stars in Globular Clusters (CVSGC) (Clement et al. 2001). The time-series VI photometry obtained in this work is reported in Table 2, of which only a small portion is included in the printed version of the paper. The full table shall be available in electronic form in the Centre de Donnés astronomiques de Strasbourg database (CDS). The variables V17, V20, V26, V27 and V31 are blended in our images and could not be resolved; therefore, they are neither included in the Table 2 nor discussed in this paper. The light curves in our data for the RRab, RRC and the SX Phe V25 are displayed in Figure 3. Our determinations of their mean magnitudes, amplitudes and periods are given in Table 3. The rms diagrams in the V and I filters and the colour-magnitude diagram (CMD) of the cluster are shown in Figures 2 and 4 respectively. The positions of the known variable stars are also shown.

⁵<http://www3.cadc-ccda.hia-ihp.nrc-cnrc.gc.ca/community/STETSON/standards>

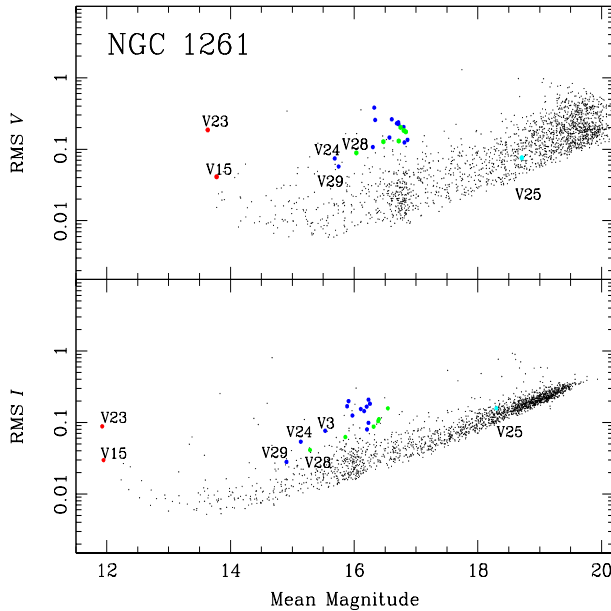


Fig. 2. rms of all light curves measured in our images as a function of the mean magnitude. Colour symbols indicate the position of the known variable stars as follows: blue and green for RRab and RRC stars respectively, red for SR stars and turquoise for the SX Phe star V25. The colour figure can be viewed online.

It is rather clear that the scatter around the horizontal branch (HB) is large and that some RR Lyrae stars appear much too bright. It is common to use the star position on the CMD as an argument against membership in the cluster, i.e., RR Lyrae stars that appear much above or below the HB. The information now available in the Gaia DR2 data base (Gaia Collaboration 2018), enables a deeper discussion on possible contamination by neighbouring unresolved stars and their proper motions. In the following section we shall refer to individual RR Lyrae stars with peculiar positions in the CMD.

Regarding the SX Phe stars, there are three of them reported in the CVSGC: V25, V26 and V30. Our light curve of V25 is shown in Figure 3. However, we have been unable to detect the faint stars V26 and V30, near the cluster core, probably because of the seeing conditions during our observations. Nevertheless, we want to point out that we see no stars, or that they are badly blended, in the positions marked in the identification chart of the discovery paper (Salinas et al. 2007).

3.1. On the Cluster Membership and Light Contamination of Individual Variables

With the aim of producing a colour-magnitude diagram (CMD) free of field stars, we applied the

TABLE 2
TIME-SERIES *VI* PHOTOMETRY FOR THE
VARIABLES STARS OBSERVED IN THIS
WORK*

Variable Star ID	Filter	HJD (d)	M_{std} (mag)	m_{ins} (mag)	σ_m (mag)
V2	V	2457985.75380	16.864	19.293	0.010
V2	V	2457985.75851	16.830	19.259	0.010
⋮	⋮	⋮	⋮	⋮	⋮
V2	I	2457985.74544	16.417	19.673	0.019
V2	I	2457985.74783	16.367	19.622	0.018
⋮	⋮	⋮	⋮	⋮	⋮
V3	V	2457985.75380	16.304	18.752	0.006
V3	V	2457985.75851	16.294	18.741	0.006
⋮	⋮	⋮	⋮	⋮	⋮
V3	I	2457985.74544	15.535	18.791	0.009
V3	I	2457985.74783	15.537	18.794	0.009
⋮	⋮	⋮	⋮	⋮	⋮

*The standard and instrumental magnitudes are listed in Columns 4 and 5, respectively, corresponding to the variable stars in Column 1. Filter and epoch of mid-exposure are listed in Columns 2 and 3, respectively. The uncertainty in m_{ins} is listed in Column 6, which also corresponds to the uncertainty on M_{std} . A full version of this table is available at the CDS database.

method of Bustos Fierro & Calderón (2019) to identify probable members in the field of the cluster. The method uses the high quality astrometric data available in Gaia DR2, and is based on the Balanced Iterative Reducing and Clustering using Hierarchies (BIRCH) algorithm (Zhang et al. 1996) in a four-dimensional space of physical parameters –positions and proper motions– that detects groups of stars in that 4D-space. We extracted 5258 Gaia sources that are very likely members of the cluster. The membership analysis shows that most of the stars in this field are indeed members of the cluster, but that their proper motions are quite small (≈ 2 mas/yr), and that their distribution overlaps well with that of the field stars. The top two panels of Figure 4 display the full CMD diagram before and after the field star correction. Almost all known variables are matched with a member. The exceptions are stars V24, V26 and V31, that match sources of unknown membership, because their proper motions were not measured in the Gaia survey.

Plotting the positions of all Gaia DR2 sources in the field of our images we noted that, in some cases, two or even three of them can fall within the FWHM of the PSF of a detected stellar source. A direct consequence of this is an alteration of the magnitude

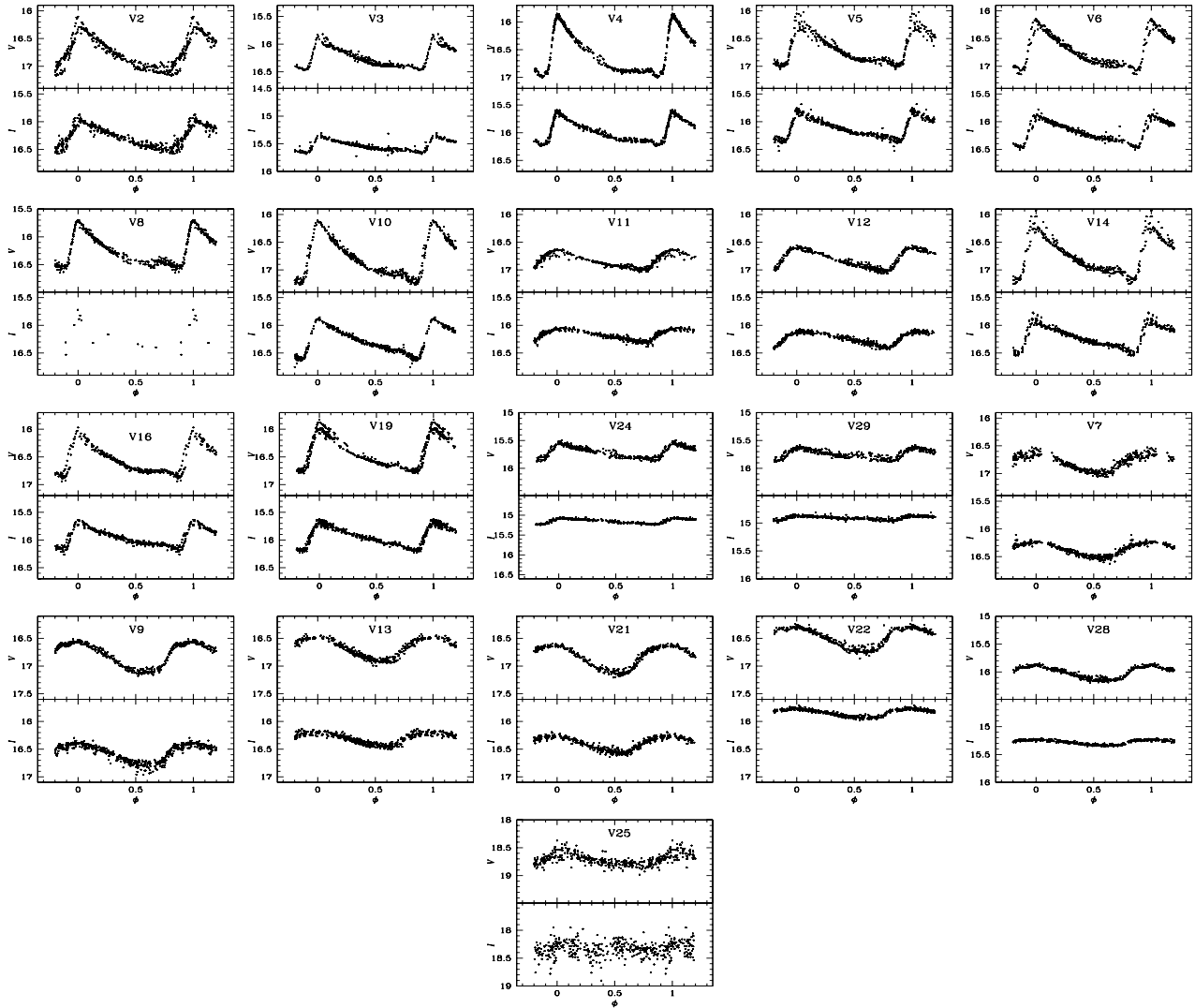


Fig. 3. VI light curves of known RRab, RRC stars and the SX Phe V25 in NGC 1261.

of the star, making it apparently brighter and, in the case of variable stars, artificially reducing the amplitude of their light curves.

In Figure 5, we show an amplification of the HB region of NGC 1261. In the left panel, known variables are plotted using the intensity weighted mean $\langle V \rangle$ and $\langle I \rangle$ listed in Table 3. RRab and RRC stars are represented by blue and green symbols respectively. It is evident that some of the RR Lyrae stars are much too bright relative to the ZAHB, namely, V3, V19, V22, V24, V28 and V29. The positions of the two RRC stars V22 and V28 are also much redder than expected. As a reference, the vertical black line that represents the empirical red edge of the first

overtone instability strip (FORE) is also displayed (Arellano Ferro et al. 2016).

To help decide whether the odd positions of these stars are the result of light pollution, or simply of their being non-members, we analysed the photometric values of all Gaia sources present in a given variable star PSF. The magnitudes of the individual sources in the Gaia photometric system, G -, G_{BP} -, and G_{RP} -band, were transformed into V and I magnitudes using the relationships provided by J.M. Carrasco (2018: Gaia team), and available in § 5.3.7 of the Gaia DR2 documentation⁶. Then, the expected combined magnitude was calculated, and hence an

⁶<http://gea.esac.esa.int/archive/documentation/GDR2/index.html>

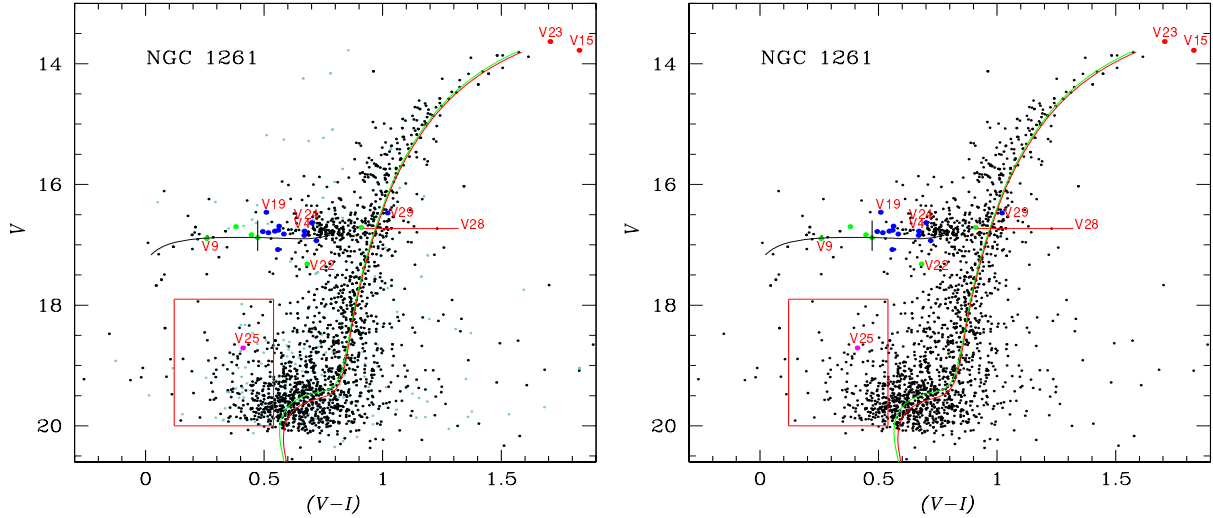


Fig. 4. Colour-magnitude diagram of NGC 1261. In the left panel, black and light blue symbols are used to distinguish between cluster members and non-members. The right panel displays only the cluster members. On the HB, blue and green symbols stand for RRab and RRC stars. Red and pink symbols represent SR and SX Phe stars. We searched for new SX Phe variables within the blue straggler region defined as the red box and found none. Isochrones and ZAHB are from the models of Vandenberg et al. (2014) for $[\text{Fe}/\text{H}]=-1.4$, $Y=0.25$ and $[\alpha/\text{Fe}]=+0.4$ for 10 and 11 Gyr, and have been shifted to a distance of 17.2 kpc, and a reddening $E(B-V)=0.01$. The colour figure can be viewed online.

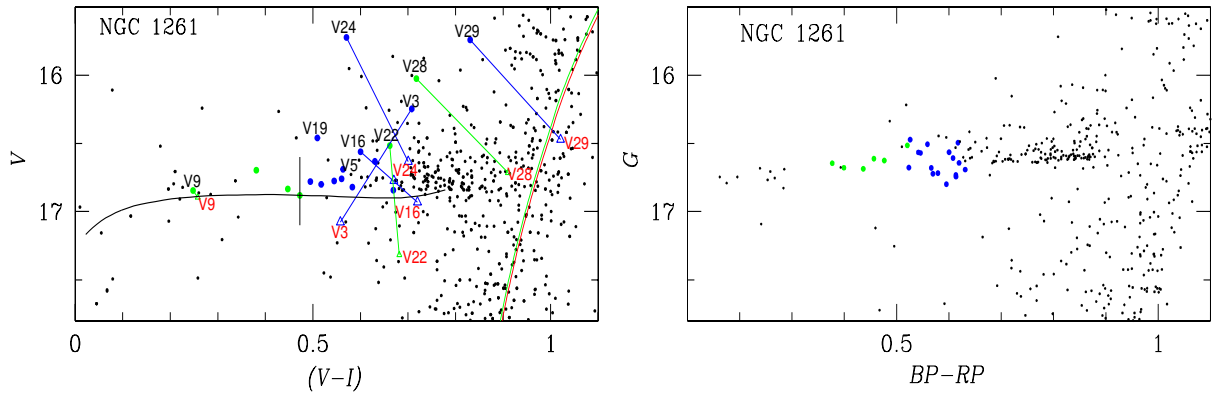


Fig. 5. Expansion of the HB branch of NGC 1261. The left panel shows the HB region built from the VI indices of this work. Labelled stars are those with more than one Gaia DR2 source within their PSF. Their corrected positions in the CMD are represented by open triangles and labelled with red numbers, see § 3.1 for details. The vertical black line is the empirical position of the red-edge first-overtone instability strip (FORE), defined by Arellano Ferro et al. (2016). (See the discussion in § 6 and § 9). The right panel shows the HB region built from the Gaia DR2 photometric indices. With the exception of the peculiar stars discussed in § 3.1 the resulting distribution of the RR Lyrae stars is comparable in both panels. The colour figure can be viewed online.

estimation was derived of the correction to be applied to our observed (combined) V and I magnitudes. This also enabled us to estimate the amplitude corrections.

In Table 4 we list the variable stars with two Gaia sources within their PSF. We used the variability flag in Gaia DR2 to identify the variable component when available; for stars without variability flag

(V17, V24 and V29) we analysed their positions in the CMD with Gaia DR2 magnitudes and colours to decide which is the variable and which is the contaminant. Their Gaia magnitudes were transformed into the Johnson-Kron-Cousins photometric system (V_{Gaia} , I_{Gaia} and $V_{\text{Gaia}} - I_{\text{Gaia}}$), and the combined magnitudes of the pair, V_{mix} and I_{mix} , were calculated. The differences between the magnitude of

TABLE 3
DATA OF VARIABLE STARS IN NGC 1261 IN THE FoV OF OUR IMAGES

Star ID	Type	$\langle V \rangle$ (mag)	$\langle I \rangle$ (mag)	A_V (mag)	A_I (mag)	P (days)	HJD _{max} + 2450000	α (J2000.0)	δ (J2000.0)	Gaia DR2 ID
V2 <i>Bl</i>	RRab	16.780	12.285	1.16	0.76	0.585730	8095.6967	03:12:11.28	-55:12:22.0	4733794790512123904
V3	RRab	16.248	15.540	0.65	0.30	0.537003	8439.8438	03:12:21.78	-55:13:50.7	4733793764014756224
V4	RRab	16.633	16.002	1.10	0.61	0.492876	8376.7150	03:12:18.56	-55:13:28.4	4733794519928245888
V5	RRab	16.690	16.127	0.96	0.64	0.513313	8012.7930	03:12:11.93	-55:13:01.9	4733794588651585664
V6 <i>Bl</i>	RRab	16.759	16.199	0.94	0.62	0.564100	8335.8557	03:12:25.05	-55:13:08.6	4733793867093968896
V7	RRc	16.835	16.388	0.47	0.32	0.333546	8095.5598	03:11:58.44	-55:10:37.3	4733797852825688704
V8	RRab	16.283	-	0.86	-	0.538204	8012.8146	03:12:00.44	-55:15:16.4	4733700580405300480
V9	RRc	16.846	16.598	0.58	0.41	0.297221	8019.6966	03:12:20.40	-55:13:35.3	4733794519928956800
V10	RRab	16.800	16.283	1.06	0.77	0.583374	8364.7012	03:12:21.99	-55:11:45.9	4733794726089585664
V11	RRab	16.843	16.174	0.39	0.26	0.662171	8335.9157	03:12:05.50	-55:11:27.7	4733794657370122880
V12	RRab	16.821	16.238	0.49	0.32	0.610285	8095.6920	03:12:26.15	-55:12:45.8	4733794657370122880
V13	RRc	16.698	16.317	0.45	0.24	0.337568	8019.7891	03:12:07.01	-55:14:33.1	4733700713548568832
V14 <i>Bl</i>	RRab	16.775	16.228	1.23	0.73	0.573977	8378.7791	03:12:09.75	-55:14:07.6	4733700717844254080
V15	SR	13.778	11.948	-	-	-	8007.7702	03:12:02.50	-55:10:48.1	4733794814168962304
V16 <i>Bl</i>	RRab	16.561	15.961	0.67	0.56	0.526160	8469.6225	03:12:13.90	-55:13:12.9	4733794588651555584
V17 ¹	RRab	-	-	-	-	0.511631	7986.8406	03:12:15.50	-55:12:36.2	4733794588651549824
V19 <i>Bl</i>	RRab	16.461	15.951	0.84	0.58	0.653738	8376.7652	03:12:18.19	-55:12:44.7	4733794691727354624
V20 ¹	RRab	-	-	-	-	-	-	03:12:19.31	-55:13:00.4	4733794623011123200
V21	RRc	16.881	16.408	0.54	0.34	0.336180	8439.8209	03:12:14.47	-55:12:31.3	4733794588651163648
V22	RRc	16.516	15.855	0.45	0.18	0.302567	8033.8565	03:12:16.49	-55:13:38.1	4733794519931924224
V23	SR	13.632	11.926	-	-	-	8055.6833	03:12:15.69	-55:12:40.7	4733794588651583616
V24	RRab	15.724	15.153	0.32	0.18	0.624395	8376.6983	03:12:14.43	-55:13:34.8	4733794554291694592
V25	SX Phe	18.710	18.300	0.25	0.18	0.056503	8033.7103	03:12:17.17	-55:11:22.7	4733794932246020480
V26 ¹	SX Phe	-	-	-	-	-	-	03:12:17.05	-55:12:43.9	4733794588651476224
V27 ¹	SR	-	-	-	-	-	-	03:12:14.63	-55:13:06.2	4733794588651284992
V28	RRc	16.025	15.285	0.25	0.11	0.287349	7986.7667	03:12:13.53	-55:13:00.8	4733794588651177344
V29 <i>Bl</i>	RRab	15.742	14.911	0.29	0.10	0.598775	7986.8960	03:12:13.05	-55:13:20.5	4733794554291844352
V30 ¹	SX Phe	-	-	-	-	-	-	03:12:16.58	-55:12:54.0	4733794588648149248
V31	EC	-	-	-	0.30	0.052493	8439.8246	03:12:18.70	-55:14:16.0	4733794519931172608

Bl: RR Lyrae with Blazhko effect.

¹Star not resolved in our images.

the variable component and the combined magnitude of the pair, ΔV and ΔI , were computed; the corrected positions are represented by triangles in the left panel of Figure 5 and labelled with red numbers. The corrected amplitudes due to the presence of the neighbour star (Amp V and Amp I) were also calculated, and are represented by colour symbols and vertical displacements in the Bailey diagram, discussed below in § 6. It can be seen in that diagram that, after the corrections of the amplitudes, most stars have moved much closer to the expected locus for this OoI type cluster.

The persistent peculiar positions of some variables in the CMD make suspicious their membership status in the cluster, or perhaps a serious light pollution by neighbouring stars is corrupting our photometry for these specific objects. In the right panel of Figure 5, we reproduced the HB of the cluster using the Gaia DR2 photometric indices. It is rewarding to see that all RR Lyrae stars fall properly on the HB, which also indicates that the selection of the true variable, performed in Table 4 for those stars contaminated by a secondary Gaia source, was

correct. This figure also shows that the distribution of modes on the HB is neatly segregated, a property that will be discussed later in the paper.

We can conclude that all known variables are most likely cluster members, and that our photometry for these stars, namely V3, V16, V19, V24, V28 and V29 is seriously contaminated by an unseen, close, well within the PSF, neighbour.

We note that the two SR V15 and V23, are members; regarding the three SX Phe, V25 lies in the blue straggler region and seems a likely member, V26 has no values for proper motion and V30 is definitely not a member. The latter two were not detected in our photometry. Hence, our calculations of the physical parameters will be restricted to the non-peculiar stars and will be described below.

3.2. Searching for New Variables

Since prolonged time-series have proven successful to identify new variables, we have performed a systematic search for them with the few strategies discussed below.

TABLE 4
VARIABLE STARS WITH TWO GAIA DR2 SOURCES WITHIN THEIR PSF*

VAR	Gaia DR2 ID	G (mag)	$G_{BP} - G_{RP}$ (mag)	V_{Gaia} (mag)	I_{Gaia} (mag)	$V_{Gaia} - I_{Gaia}$ (mag)	V_{mix} (mag)	ΔV (mag)	I_{mix} (mag)	ΔI (mag)	Amp V (mag)	Amp I (mag)
V3	4733793764014756224	16.6773	0.5234	16.746	16.295	0.451	15.91	0.83	15.32	0.98	1.39	0.74
V3	4733793764014757248	16.4500	0.8248	16.591	15.883	0.708	–	–	–	–	–	–
V4	4733794519928245888	16.5663	0.5417	16.638	16.172	0.467	16.50	0.14	16.07	0.10	1.26	0.67
V4	4733794519931768192	18.7558	–	18.773	18.735	0.038	–	–	–	–	–	–
V9	4733794519928956800	16.6788	0.3993	16.727	16.377	0.350	16.67	0.05	16.34	0.04	0.61	0.43
V9	4733794519928957056	19.9313	–	19.949	19.910	0.038	–	–	–	–	–	–
V16	4733794588651555584	16.5656	0.6003	16.650	16.134	0.516	16.28	0.37	15.88	0.25	–	–
V16	4733794588651555840	17.6072	–	17.625	17.586	0.038	–	–	–	–	–	–
V17	4733794588651549824	16.6079	0.6079	16.694	16.172	0.522	15.76	0.93	15.14	1.03	–	–
V17	4733794588651550080	16.2219	0.7993	16.356	15.670	0.686	–	–	–	–	–	–
V22	4733794519931924224	16.6257	0.4764	16.686	16.273	0.413	15.89	0.80	15.49	0.78	0.91	0.37
V22	4733794519931924352	16.5920	0.6806	16.592	16.217	0.375	–	–	–	–	–	–
V24	4733794554291694592	16.4950	0.6173	16.583	16.053	0.530	15.67	0.91	15.27	0.78	0.73	0.36
V24	4733794554291623424	16.2512	0.3297	16.290	15.996	0.294	–	–	–	–	–	–
V27	4733794588651284992	16.5018	0.5269	16.571	16.117	0.454	16.33	0.24	15.94	0.17	–	–
V27	4733794588651285376	18.0489	–	18.067	18.028	0.038	–	–	–	–	–	–
V28	4733794588651177344	16.5151	0.5204	16.583	16.134	0.449	15.89	0.69	15.62	0.52	0.48	0.18
V28	4733794588651552256	16.6861	–	16.704	16.665	0.038	–	–	–	–	–	–
V29	4733794554291844352	16.5704	0.5458	16.588	16.550	0.038	15.92	0.73	15.64	0.54	–	–
V29	4733794554291843840	16.6775	–	16.695	16.657	0.038	–	–	–	–	–	–

*For every pair, the Gaia DR2 source in the first line is the variable and the one in the second line is the contaminant. See § 3.1 for details.

On the CMD of NGC 1261, we isolated all stars contained in regions where it is common to find variable stars, e.g. near the instability strip (IS) in the horizontal branch (HB), the blue straggler region (BS) and near the tip of the red giant branch (TRGB). We analysed the light curves of the stars in those regions and looked for variability by determining their period (if any), using the program PERIOD04 (Lenz & Breger 2005) or the string-length method (Burke et al. 1970; Dworetzky 1983); then, we plotted their apparent magnitudes with respect to their phase. For long-term variables, the magnitude is plotted as a function of heliocentric Julian day in search for hints of variability. This procedure recovered all known variables, but we found no new ones in our data.

Another method consists in the detection of variations of PSF-like peaks in stacked residual images, from which we can see the variable stars blink. Again, all previous known variables were detected, but no new variables emerged.

3.3. About the RR Lyrae Stars from Gaia DR2 in the Field of NGC 1261

In their catalogue of RR Lyrae stars identified via the Specific Object Study pipeline in Gaia DR2 all over the sky, Clementini et al. (2019) report

21 RR Lyrae stars within a radius of 20 arcmin around NGC 1261. Eighteen of these are known RR Lyrae stars listed in the CVSGC. Two stars, well in the outskirts of that field, (Gaia DR2 sources 4734551739843543808 and 4733801701116515200), are not members according to the method of Bustos Fierro & Calderón (2019) and are not in the field of our observations. A third star near the cluster core (Gaia DR2 source 4733794519931744000), categorised by Clementini et al. (2019) as an RRc star, is present in our light curve collection. We identified it as C1 in the chart of Figure 7, but we found no variations. The star, with mean magnitudes $V=16.35$ and $I=15.63$, lies somewhat above the red clump. Thus, we do not confirm it as an RRc star.

For clarification, we offer in Figure 7 an identification chart of all variables reported in the CVSGC. The SX Phe stars V26 and V30, although identified according to the coordinates in the CVSGC, were not resolved in the photometry of the present study.

4. BAILEY DIAGRAM AND OOSTERHOFF TYPE

The period-amplitude or Bailey diagram for RR Lyrae stars is shown in Figure 6 for the VI bandpasses. The periods and amplitudes are listed in Table 3. In most cases, we took the amplitudes cor-

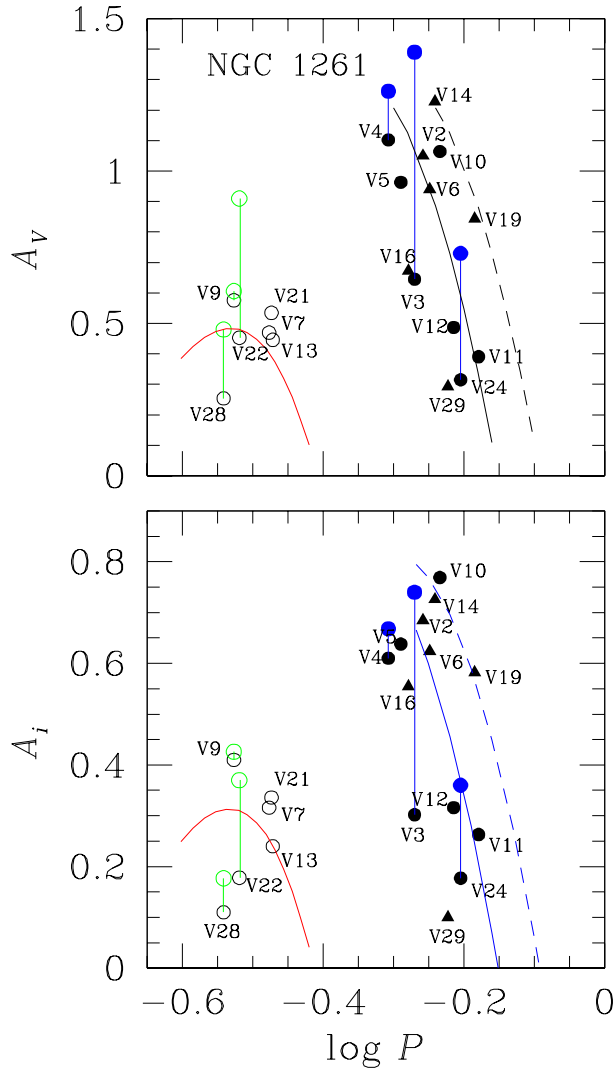


Fig. 6. Period-Amplitude diagram for NGC 1261. The amplitudes of a few variables have been corrected for the presence of an unresolved neighbour. These are plotted with green and blue symbols for RRc and RRab stars, respectively. Triangles are used for Blazhko variables. The distribution of stars is characteristic of Oo I type clusters. See § 3.1 and § 4 for details. The colour figure can be viewed online.

responding to the best fit provided by the Fourier decomposition of the light curves. In cases where the light curve showed Blazhko effect, the maximum amplitude was measured and the star was plotted with a triangular marker. The continuous and dashed black lines in the top panel of Figure 6 are the loci for unevolved and evolved stars according to Cacciari et al. (2005). The red parabolas were calculated by Arellano Ferro et al. (2015) from a sample of RRc stars in five OoI clusters, avoiding Blazhko variables. In the

bottom panel, the blue solid and segmented loci for unevolved and evolved stars, respectively, are taken from Kunder et al. (2013).

As noted in § 3.1, a few variables are clearly unresolved from very close neighbours. In these cases, the amplitudes were corrected using the individual magnitudes of the components listed in Table 4. The corrected amplitudes are indicated in Figure 6 by green and blue symbols for RRc and RRab stars, respectively. It is rather clear that the amplitude corrections help sustain the fact that the distribution of stars concentrates around the unevolved sequences, as expected for Oo I type clusters.

5. COMMENT ON THE CLUSTER REDDENING

While this cluster is far away from the Galactic disk, and a very low reddening has been assigned to it, it is always a good exercise to calculate the reddening by an independent method. Individual reddenings for RRab stars can be estimated using the colour curve near minimum. Proposed originally by Sturch (1966), the method has now been calibrated in the VI passbands by Guldenschuh et al. (2005), who concluded that the intrinsic colour $(V - I)_0$ of RRab stars curves at phases 0.5-0.8, is 0.58 ± 0.02 . We calculated the observed $(V - I)$ at this phase range in our light curves and estimated individual values of $E(V - I)$, the average of which, converted to $E(B - V) = E(V - I)/1.259$ is 0.055 ± 0.051 , i.e., nearly zero, and in agreement with the interstellar reddening of $E(B - V) = 0.01$ given by the calibrations of Schlafly & Finkbeiner (2011) and Schlegel et al. (1998). In what follows we shall adopt $E(B - V) = 0.01$.

6. RR LYRAE STARS: [Fe/H] AND M_V FROM LIGHT CURVE FOURIER DECOMPOSITION

Fourier decomposition of the light curves and the use of empirical calibrations enable us to estimate some key physical stellar parameters. The Fourier series to mathematically describe the light curve is of the form:

$$m(t) = A_0 + \sum_{k=1}^N A_k \cos\left(\frac{2\pi}{P}k(t - E_0) + \phi_k\right), \quad (3)$$

where $m(t)$ is the magnitude at time t , P is the period of pulsation, and E_0 is the epoch. When calculating the Fourier parameters, we used a least-squares approach to estimate the best fit for the amplitudes A_k and phases ϕ_k of the light curve components. The phases and amplitudes of the harmonics

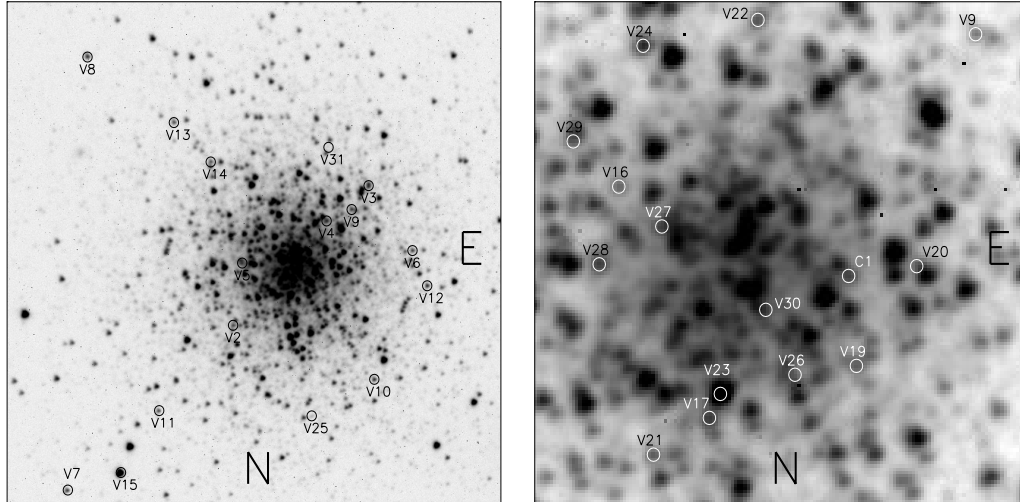


Fig. 7. Identification charts of all known variables in NGC 1261. The field of the left chart is $5.4' \times 5.4'$, and the cluster core on the right chart is $1.3' \times 1.3'$. The star labelled C1 is the one listed as an RR Lyrae by Clementini et al. (2019), but in this work it is found to be non-variable (cf. § 3.3).

TABLE 5

FOURIER COEFFICIENTS A_K FOR $K = 0, 1, 2, 3, 4$, AND PHASES ϕ_{21} , ϕ_{31} AND ϕ_{41} , FOR RRab AND RRc STARS*

Variable ID	A_0 (V mag)	A_1 (V mag)	A_2 (V mag)	A_3 (V mag)	A_4 (V mag)	ϕ_{21}	ϕ_{31}	ϕ_{41}
RRab stars								
V2	16.788(4)	0.331(6)	0.126(6)	0.072(6)	0.029(6)	4.036(59)	8.198(99)	6.147(219)
V6	16.752(2)	0.305(4)	0.146(4)	0.098(3)	0.070(4)	3.910(33)	8.215(51)	6.205(68)
V10	16.810(3)	0.377(4)	0.189(3)	0.128(4)	0.077(4)	3.936(27)	8.255 (39)	6.191(59)
V11	16.837(3)	0.147(4)	0.060(3)	0.028(4)	0.011(4)	4.050(78)	8.587 (139)	7.709(344)
V12	16.816(2)	0.177(3)	0.070(3)	0.034(3)	0.018(3)	4.406(48)	9.254(90)	7.522(150)
V14	16.775(3)	0.368(5)	0.182(4)	0.154(5)	0.088(5)	4.079(39)	8.369 (51)	6.378(75)
RRc stars								
V7	16.810(3)	0.181(4)	0.011(4)	0.019(4)	0.008(4)	4.665(31)	4.415(201)	2.409(509)
V9	16.846(1)	0.285(2)	0.052(2)	0.028(2)	0.028(2)	4.749(37)	2.734(64)	1.485(67)
V13	16.698(2)	0.222(3)	0.026(3)	0.013(3)	0.008(2)	4.792(114)	3.815(206)	2.681(318)
V21	16.881(1)	0.262(2)	0.022(2)	0.023(2)	0.006(2)	4.795(88)	4.115(88)	2.729(347)

*The numbers in parentheses indicate the uncertainty of the last decimal places.

in equation 3, i.e. the Fourier parameters, are defined as $\phi_{ij} = j\phi_i - i\phi_j$, and $R_{ij} = A_i/A_j$.

This approach has been regularly used for RR Lyrae stars in a large number of clusters (e.g., Arellano Ferro et al. (2018a); Deras et al. (2019) and references therein). To avoid a lengthy repetition, we refer the reader to § 4 of Deras et al. (2019) for the specific calibrations. Particularly, their equations 4 and 5 describe the calibrations for RRab stars of Jurcsik & Kovács (1996) and Kovács & Walker (2001), which render values of $[\text{Fe}/\text{H}]$ and M_V , with standard deviations of 0.14 dex and 0.04 mag respec-

tively, and to equations 6 and 7, that give the calibrations for RRc stars of Morgan et al. (2007) and Kovács & Kanbur (1998) with standard deviations of 0.14 dex and 0.042 mag respectively. We have not included in the calculation of physical parameters those stars that are apparently contaminated by a neighbouring source (cf. § 3.1); since the presence of a neighbour also perturbs the light curve shapes and the Fourier parameters, so that the derived physical parameters become spurious. In Table 5 we list the Fourier parameters, and in Table 6 the corresponding individual physical parameters for the

TABLE 6
PHYSICAL PARAMETERS FROM THE FOURIER FIT FOR RRab AND RRc STARS*

RRab stars							
Star	[Fe/H] _{ZW}	[Fe/H] _{UVES}	M_V	$\log T_{\text{eff}}$	$\log(L/L_{\odot})$	M/M_{\odot}	R/R_{\odot}
V2	-1.46(9)	-1.37(10)	0.570(9)	3.811(25)	1.672(3)	0.70(21)	5.49(2)
V6	-1.49(5)	-1.40(5)	0.604(5)	3.809(10)	1.658(3)	0.67(8)	5.46(1)
V10	-1.53(4)	-1.44(4)	0.517(6)	3.810(10)	1.693(2)	0.70(8)	5.66(2)
V11	-1.51(13)	-1.43(14)	0.600(6)	3.790(39)	1.660(2)	0.67(31)	5.98(2)
V12	-0.69(9)**	-0.67(4)**	0.635(4)	3.813(18)	1.646(2)	0.55(12)	5.29(1)
V14	-1.39(5)	-1.28(5)	0.562(7)	3.812(11)	1.675(3)	0.66(9)	5.49(2)
Weighted Mean	-1.48	-1.38	0.590	3.810	1.664	0.66	5.51
$\sigma_{\bar{x}}$	± 0.05	± 0.05	± 0.042	± 0.008	± 0.006	± 0.05	± 0.09
RRc stars							
Star	[Fe/H] _{ZW}	[Fe/H] _{UVES}	M_V	$\log T_{\text{eff}}$	$\log(L/L_{\odot})$	M/M_{\odot}	R/R_{\odot}
V7	-1.06(42)	-0.95(32)	0.571(18)	3.869(1)	1.672(7)	0.49(1)	4.21(4)
V9	-1.63(11)	-1.57(13)	0.512(9)	3.866(1)	1.695(4)	0.63(1)	4.37(2)
V13	-1.50(41)	-1.41(44)	0.588(10)	3.864(1)	1.677(4)	0.51(1)	4.47(2)
V21	-1.31(18)	-1.19(17)	0.571(10)	3.866(1)	1.672(4)	0.49(1)	4.25(2)
Weighted Mean	-1.51	-1.38	0.547	3.866	1.681	0.54	4.31
$\sigma_{\bar{x}}$	± 0.29	± 0.29	± 0.014	± 0.001	± 0.005	± 0.03	± 0.05

*The numbers in parentheses indicate the uncertainty on the last decimal places. See § 6 for a detailed discussion.

**Not included in the average of [Fe/H].

stars included in the calculation and the average values. For comparison, we have transformed [Fe/H]_{ZW} on the Zinn & West (1984) metallicity scale into the UVES scale using the equation [Fe/H]_{UVES} = -0.413 + 0.130 [Fe/H]_{ZW} - 0.356 [Fe/H]_{ZW}² (Carretta et al. 2009). It should be noted that the uncertainties we have quoted in Table 6 only represent the internal errors associated to the Fourier fitting procedure, and do not include any systematic errors that may be inherent to the use of the calibrations quoted above to estimate the physical parameters. The standard deviation of the mean $\sigma_{\bar{x}}$, given below the weighted mean physical parameters, is comparable to the standard deviation of the calibrations, and represents a more reliable estimate of the systematic errors in our procedure.

7. PREVIOUS METALLICITY ESTIMATES OF NGC 1261

To our knowledge, no spectroscopic determination of the metallicity of NGC 1261 or of any of its stars has ever been published. Estimations of [Fe/H] based on photometric indices and their calibrations do exist; they use the height above the HB, the slope of the HB, and the intrinsic colour ($B-V$)₀ of the reg-giant branch (RGB) at the HB level. Ferraro et al. (1993) employed these methods and found -1.54 ± 0.4 , -1.85 ± 0.2 and -1.26 ± 0.04 respectively, adopting a weighted average -1.4 ± 0.2 . The value of

[Fe/H] listed in the catalogue of Harris (1996) (2010 edition) is -1.27 , which corresponds to the compiled average of Carretta et al. (2009) in their UVES scale, which is equivalent to -1.4 ± 0.2 in the Zinn-West scale.

Our results, based on the Fourier decomposition and calibrations discussed in § 6 and listed in Table 6 are, for the RRab stars: [Fe/H]_{ZW} = -1.48 ± 0.05 or [Fe/H]_{UVES} = -1.38 ± 0.05 , and for the RRc stars: [Fe/H]_{ZW} = -1.51 ± 0.29 or [Fe/H]_{UVES} = -1.38 ± 0.29 . Since different empirical relations have been used to estimate the metallicities of the RRab and RRc stars, there may be some systematic offset between the metallicity estimates for the two types of variable. We should note the peculiarly large value of [Fe/H] found for star V12. The reason for this is the anomalously large value of the Fourier parameter ϕ_{31} of 9.254 ± 0.09 . Star V12 is among the smallest amplitude and largest period RRab in NGC 1261, and reminds us of the case of star V12 in NGC 6171, whose light curve structure is different from that of other RRab stars (Clement & Shelton 1997), and thus is not suitable for the calculation of [Fe/H] from the Fourier analysis. Although the associated uncertainties of our average values of [Fe/H] are smaller than those of previous determinations, the values are slightly more metal-weak than those published; still, they are rather in agreement, within the given uncertainties.

8. ON THE DISTANCE TO NGC 1261

The solar distance to NGC 1261 recorded in the catalogue of Harris (1996) (2010 edition) is 16.3 kpc, calculated from the estimated mean $V = 16.70 \pm 0.05$ level HB of Ferraro et al. (1993), adopting a $[\text{Fe}/\text{H}]$ - M_V relation with $[\text{Fe}/\text{H}]$ and $E(B - V) = 0.01$. Our Fourier estimates of M_V and $\langle V \rangle$ for RRab and RRC stars lead to mean distances of 17.2 ± 0.4 and 17.6 ± 0.7 kpc respectively. Considering that the scatter of the 6 RRC stars in the CMD is large, and that we only used the RRab closer to the ZAHB, we should probably ignore the distance obtained from the RRC stars, in which case our best estimate of the distance to the cluster from this method is 17.2 ± 0.4 kpc. In Figure 4 we have shifted the ZAHB and isochrones to this distance, although, admittedly an eye fit of the HB suggests a brighter ZAHB for a distance of about 16.8 kpc

Another independent method to estimate the distance to the cluster is via the P-L relations of SX Phe stars and of RR Lyrae stars. In the former case, we have calculated M_V of the star V25, the only SX Phe detected in our study, using three versions of the P-L relations from Cohen & Sarajedini (2012), Poretti et al. (2008) and Arellano Ferro et al. (2011), and found 16.1, 15.5 and 15.0 kpc respectively, i.e., all values well below the estimates based on the HB luminosity.

Alternatively, the P-L in the I -band for RR Lyrae stars derived by Catelan et al. (2004); $M_I = 0.471 - 1.132 \log P + 0.205 \log Z$, with $\log Z = [M/H] - 1.765$; $[M/H] = [\text{Fe}/\text{H}] - \log(0.638 f + 0.362)$ and $\log f = [\alpha/\text{Fe}]$ (Salaris et al. 1993), was applied to the RRab and RRC stars residing close to the ZAHB in the CMD of Figure 4. From 6 RRab and 4 RRC stars we found an average distance of 16.65 ± 0.27 kpc, which agrees very well with the results obtained from the Fourier light curve decomposition approach. In summary, the best results for the cluster distance are obtained from the Fourier light curve decomposition of the RRab stars that show little scatter near the ZAHB, and the P-L (I) relationship; these methods give an average of 16.7 kpc and an uncertainty between 0.7 and 0.3 kpc, respectively.

9. STRUCTURE OF THE HB AND AGE

NGC 1261 has a very red HB. The HB structure can be characterised by the parameter $\mathcal{L} \equiv (B - R)/(B + V + R) = -0.67$. In the HB region shown in the left panel of Figure 5, built from our VI indices, the RRab and RRC stars appear

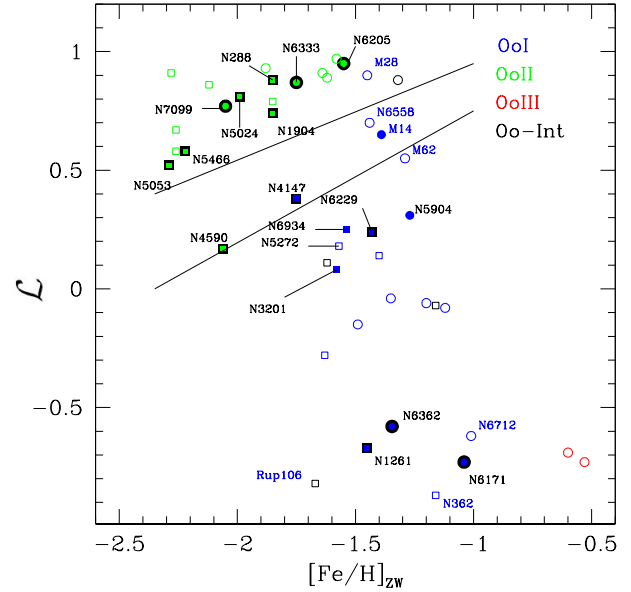


Fig. 8. The HB structure parameter \mathcal{L} as function of $[\text{Fe}/\text{H}]$. Circles and squares are used for inner and outer halo clusters, respectively. The black-rimmed symbols represent globular clusters where the fundamental and first overtone modes are well segregated around the FORE, as opposed to filled non-rimmed symbols. The upper and lower solid lines are the limits of the Oosterhoff gap according to Bono et al. (1994). Empty symbols are clusters not yet studied by our group. The colour figure can be viewed online.

clearly well segregated by the FORE. This is confirmed in the right panel, built with the Gaia DR2 indices. Figure 8 is an updated version of Figure 9 of Arellano Ferro et al. (2018b) which includes NGC 1261 and a few other clusters. Clearly NGC 1261, like other Oo I clusters with very red HBs like NGC 6171 (M107) and NGC 6362, shows a neat segregation of pulsation modes among the RR Lyrae stars. Other Oo I clusters with a similarly red HB where the RRC-RRab distribution is yet to be explored are: NGC 362, Rup 106 and NGC 6712. In Rup 106, however, no RRC stars are known, and NGC 6712 is an interesting borderline case, since either a few RRab are sitting in the either-or region, or the FORE is shifted to the red by only about 0.04 mag (Deras 2019; private communication), which is the uncertainty in the location of the FORE. We have found that in all Oo II clusters the modes are always segregated. Only a few Oo I clusters with \mathcal{L} between 0.0 and 0.7 have been found to have the inter-mode region populated by RRab and RRC stars: NGC 3201, NGC 5904 (M5), NGC 6402 (M14) and NGC 6934.

Based on Hubble Space Telescope Advanced Camera for Surveys photometry, and using the isochrone fitting between the base of the turnoff and the lower RGB, VandenBerg et al. (2013) concluded that the age of NGC 1261 is 10.75 ± 0.25 Gyr. Since the precision of our photometry, and the dispersion in the CMD near the TO are inadequate for a subtle discussion of the age of the system, we overplotted on our observed CMD two isochrones for 10.0 and 11.0 Gyr from the *Victoria – Regina* stellar models of VandenBerg et al. (2014), for $[\text{Fe}/\text{H}] = -1.4$, $Y = 0.25$ and $[\alpha/\text{Fe}] = 0.4$. The isochrones and the ZAHB, shifted to a distance of 17.2 kpc and $E(B - V) = 0.01$. We can see (Figure 4) that the current data set is consistent with the age of the cluster determined by VandenBerg et al. (2013).

10. SUMMARY AND DISCUSSION

Almost all photometric studies of NGC 1261, both in the photographic plate and CCD eras, dedicated their efforts to the overall study of the cluster, its CMD structure and the estimation of its age. Only a few studies, since the pioneering works of Fourcade & Laborde (1966) and Laborde & Fourcade (1966) when the first variables in this cluster were discovered, have been devoted to the study of the cluster variable stars population. Specifically, in the CCD era and to the best of our knowledge, only the works of Salinas et al. (2007) and Salinas et al. (2016) have focused on the study of the variable stars in crowded environments, via the differential image approach (DIA). Yet these authors point out the extreme difficulty of transforming the relative fluxes rendered by DIA, into the astrophysically more useful magnitudes of a given calibrated system. We must add that time-series do not always fully cover the light curves in the phase diagrams. The present study is the first one, as far as we know, that reports complete light curves in the VI filters, and use them to derive physical quantities from the variable star families of NGC 1261. This approach also allows our best estimate of the cluster distance to be 17.2 ± 0.4 kpc. Individual radii and masses for the RR Lyrae stars are also reported.

A thorough multi-approach search in a region of about $10' \times 10'$ around the cluster revealed no new variable stars within the limitations of our CCD photometry. The Fourier decomposition technique was employed to derive the mean values $[\text{Fe}/\text{H}]_{\text{UVES}} = -1.38 \pm 0.05$ and $[\text{Fe}/\text{H}]_{\text{UVES}} = -1.38 \pm 0.29$ for the RRab and RRc stars, respectively. These values are given in the high dispersion spectroscopic scale

established by Carretta et al. (2009). These two estimations should be considered independent, as they come from totally unrelated calibrations. The above results show a cluster slightly more metal poor and distant than generally accepted (e.g., Harris 1996).

The distribution of cluster member RR Lyrae stars on the HB shows a rather clear split of modes about the FORE, as seems to be the case for another two or perhaps three globulars with very red HB, namely, NGC 6171, NGC 6362 and probably NGC 6712. Two more clusters with a very red HB are NGC 362 and Rup 106, but no detailed study of the distribution of modes exists for NGC 362, and no RRc stars are known in Rup 106.

We are grateful to Cecilia Quiñones for her proficient help during the acquisition of the observations in Bosque Alegre. This project was partially supported by DGAPA-UNAM (Mexico) via grant IN104917-19. We have made extensive use of the SIMBAD, ADS services.

REFERENCES

- Arellano Ferro, A., Ahumada, J. A., Bustos Fierro, I. H., Calderón, J. H., & Morrell, N. I. 2018a, AN, 339, 183
 Arellano Ferro, A., Figuera Jaimes, R., Giridhar, S., et al. 2011, MNRAS, 416, 2265
 Arellano Ferro, A., Luna, A., Bramich, D. M., 2016, Ap&SS, 361, 175
 Arellano Ferro, A., Mancera Piña, P. E., Bramich, D. M., et al. 2015, MNRAS, 452, 727
 Arellano Ferro, A., Rojas Galindo, F. C., Muneer, S., & Giridhar, S. 2018b, RMxAA, 54, 325
 Bartolini, C., Grilli, F., & Robertson, J. W. 1971, IBVS, 594, 1
 Bono, G., Caputo, F., & Stellingwerf, R. F. 1994, ApJ, 423, 294
 Bramich, D. M. 2008, MNRAS, 386, L77
 Bramich, D. M., Bachelet, E., Alsubai, K. A., Mislis, D., & Parley, N. 2015, A&A, 577, A108
 Bramich, D. M., Figuera Jaimes, R., Giridhar, S., & Arellano Ferro, A. 2011, MNRAS, 413, 1275
 Bramich, D. M. & Freudling, W. 2012, MNRAS, 424, 1584
 Bramich, D. M., Horne, K., Albrow, M. D., et al. 2013, MNRAS, 428, 2275
 Burke, Edward W., J., Rolland, W. W., & Boy, W. R. 1970, JRASC, 64, 353
 Bustos Fierro, I. H. & Calderón, J. H. 2019, MNRAS, 488, 3024
 Cacciari, C., Corwin, T. M., & Carney, B. W. 2005, AJ, 129, 267
 Caputo, F., Castellani, V., & Tornambe, A. 1978, A&A, 67, 107
 Carretta, E., Bragaglia, A., Gratton, R., D'Orazi, V., & Lucatello, S. 2009, A&A, 508, 695

- Catelan, M., Pritzl, B. J., & Smith, H. A. 2004, *ApJS*, 154, 633
- Clement, C. M., Muzzin, A., Dufton, Q., et al. 2001, *AJ*, 122, 2587
- Clement, C. M. & Shelton, I. 1997, *AJ*, 113, 1711
- Clementini, G., Ripepi, V., Molinaro, R., et al. 2019, *A&A*, 622, A60
- Cohen, R. E. & Sarajedini, A. 2012, *MNRAS*, 419, 342
- Deras, D., Arellano Ferro, A., Lázaro, C., et al. 2019, *MNRAS*, 486, 2791
- Dworetzky, M. M. 1983, *MNRAS*, 203, 917
- Ferraro, F. R., Clementini, G., Fusi-Pecci, F., Vitiello, E., & Buonanno, R. 1993, *MNRAS*, 264, 273
- Fourcade, C. R. & Laborde, J. R. 1966, *Atlas y Catálogo de Estrellas Variables en Cúmulos globulares al sur de -29°, Córdoba, Argentina*
- Gaia Collaboration, Brown, A. G. A., Vallenari, A., et al. 2018, *A&A*, 616, A1
- Goldsbury, R., Richer, H. B., Anderson, J., et al. 2010, *AJ*, 140, 1830
- Guldenschuh, K. A., Layden, A. C., Wan, Y., et al. 2005, *PASP*, 117, 721
- Harris, W. E. 1996, *AJ*, 112, 1487
- Jurcsik, J. & Kovács, G. 1996, *A&A*, 312, 111
- Kovács, G. & Kanbur, S. M. 1998, *MNRAS*, 295, 834
- Kovács, G. & Walker, A. R. 2001, *A&A*, 374, 264
- Kunder, A., Stetson, P. B., Cassisi, S., et al. 2013, *AJ*, 146, 119
- Laborde, J. R. & Fourcade, C. R. 1966, *MmSAI*, 37, 251
- Lenz, P. & Breger, M. 2005, *CoAst*, 146, 53
- Morgan, S. M., Wahl, J. N., & Wieckhorst, R. M. 2007, *MNRAS*, 374, 1421
- Poretti, E., Clementini, G., Held, E. V., et al. 2008, *ApJ*, 685, 947
- Salaris, M., Chieffi, A., & Straniero, O. 1993, *ApJ*, 414, 580
- Salinas, R., Catelan, M., Smith, H. A., & Pritzl, B. J. 2007, *IBVS*, 5744
- Salinas, R., Contreras Ramos, R., Strader, J., et al. 2016, *AJ*, 152, 55
- Schlafly, E. F. & Finkbeiner, D. P. 2011, *ApJ*, 737, 103
- Schlegel, D. J., Finkbeiner, D. P., & Davis, M. 1998, *ApJ*, 500, 525
- Stetson, P. B. 2000, *PASP*, 112, 925
- Sturch, C. 1966, *ApJ*, 143, 774
- VandenBerg, D. A., Bergbusch, P. A., Ferguson, J. W., & Edvardsson, B. 2014, *ApJ*, 794, 72
- VandenBerg, D. A., Brogaard, K., Leaman, R., & Casagrande, L. 2013, *ApJ*, 775, 134
- Wehlau, A. & Demers, S. 1977, *A&A*, 57, 251
- Wehlau, A., Flemming, T., Demers, S., & Bartolini, C. 1977, *IBVS*, 1361
- Zhang, T., Ramakrishnan, R., & Livny, M. 1996, *BIRCH: An Efficient Data Clustering Method for Very Large Databases*, ed. J. Widom, in *Proceedings of the 1996 ACM SIGMOD International Conference on Management of Data*, 103
- Zinn, R. & West, M. J. 1984, *ApJS*, 55, 45

- J. A. Ahumada, I. H. Bustos Fierro, and J. H. Calderón: Universidad Nacional de Córdoba, Observatorio Astronómico, Córdoba, Argentina (ivanbf, calderon@oac.unc.edu.ar), (javier.ahumada@unc.edu.ar).
- A. Arellano Ferro: Instituto de Astronomía, Universidad Nacional Autónoma de México, Apartado Postal 70-264, México, CDMX, C.P. 04510 (armando@astro.unam.mx).
- J. H. Calderón: Consejo Nacional de Investigaciones Científicas y Técnicas (CONICET), Buenos Aires, Argentina (calderon@oac.unc.edu.ar).