

## AVOIDING MURPHY'S LAW ON DETECTING METEORS

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### ABSTRACT

It is known that when a meteoroid has been imaged by two or more stations, its atmospheric trajectory can be inferred. In addition to this, if the velocity of the meteor has been measured, then the magnitude, the photometric mass and its orbital elements can be computed. Hence, meteor detection networks have a large number of stations. Unfortunately, weak meteors are only imaged by the nearest station, since the brightness decreases with the square of the distance. On the other hand, Murphy's law can act in the event of brilliant meteors and fireballs: "In a station it was cloudy. In another, the fireball was hidden under the horizon. A third was out of order due to an electrical power failure, and the other was under maintenance, etcetera." Do not panic. In this work we present some methods to obtain information from a meteor seen from a single station, if it has been possible to associate it with a meteor shower. In this work, CCD images gathered by the robotized networks of the Sociedad Malagueña de Astronomía (Aznar 2016) and the BOOTES-1 and -2 observatories have been used (Castro-Tirado et al. 2008).

### RESUMEN

Es conocido que cuando un meteoroide ha sido captado por dos o más estaciones, su trayectoria atmosférica puede ser inferida. Además, si la velocidad del meteoroide ha sido medida, entonces su magnitud, masa fotométrica y elementos orbitales pueden ser calculados. De ahí que las redes de detección de meteoros consten de un gran número de estaciones. Por desgracia, los meteoros débiles son solo detectados por la estación más cercana, ya que su brillo decrece con el cuadrado de la distancia. Por otro lado, la Ley de Murphy puede actuar incluso en los casos de meteoros brillantes y bolas de fuego: "En una estación estuvo nublado. En otra la bola de fuego se ocultó bajo el horizonte. Una tercera se encontraba fuera de servicio debido a un fallo en el suministro eléctrico o por labores de mantenimiento, etcétera." Que no cunda el pánico. En este artículo presentamos algunos métodos para obtener información de un meteoroide visto desde una sola estación, siempre que haya sido posible asociarlo a una lluvia de estrellas. Las imágenes utilizadas han sido capturadas por la redes robotizadas de la Sociedad Malagueña de Astronomía (Aznar 2016) y los observatorios BOOTES-1 y 2 (Castro-Tirado et al. 2008).

*Key Words:* meteorites, meteors, meteoroids

### 1. A PERSEID DETECTED BY TWO STATIONS

To test the method described in later sections we used as an example a Perseid detected on August 13, 2017 by two all-sky cameras (one at SMA/OAT (Aznar 2016) and another one at the BOOTES-2 station (Castro-Tirado et al. 2008)) and a video camera (also at SMA/OAT) (see Figures 1 and 2).

From the observations of the event it is possible to calculate its atmospheric trajectory of the meteoroid, its speed and, of these, its magnitude and

photometric mass. The methods used for this are well known and can be consulted, for instance, in Ceplecha (1987), Dubyago (1961), and Borovička et al. (1995). The results are summarized in the Table 1.

### 2. ONLY SINGLE STATION AND KNOWN TIME

A meteoroid has been seen from station S. The starting and ending points (*B* and *F*) projected onto the celestial sphere determine a maximum circumference (Figure 3). If the radiant of an active meteor shower is close to this circumference, it is logical to suspect that the meteoroid is associated with such shower. Let *R'* be the closest point to the radiant *R*. The distance between *S* and the vector  $\overrightarrow{BF}$  is unknown. But if we have time tagged the duration *t* of the meteor, the module of that vector should be  $m = vt$ , where *v* is the typical speed of the associ-

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Fig. 1. Perseid on August 13 from BOOTES-2.

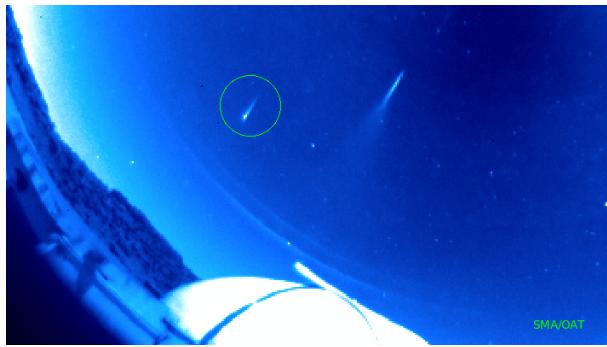


Fig. 2. Perseid on August 13 from OAT.

ated shower. Therefore, it is possible to compute a vector of module  $m$ , with origin in the line  $\overline{SB'}$  and end in the line  $\overline{SF'}$ , whose direction is the opposite of the apparent radiant  $R'$ .

Indeed. The coordinates of the vector  $\overrightarrow{BF}$  are

$$-(m \cos(\delta) \cos(\alpha), m \cos(\delta) \sin(\alpha), m \sin(\delta)),$$

where  $(\alpha, \delta)$  are the equatorial coordinates of  $R'$ . The vector  $\overrightarrow{SB}$  is obtained as a linear combination  $\overrightarrow{SB} = \overrightarrow{OS} + \lambda_b v_b$ , where  $\lambda_b$  is the distance between the station  $S$  and  $B$ ,  $v_b$  is an unitary vector  $(\cos(\delta_b) \cos(\alpha_b), \cos(\delta_b) \sin(\alpha_b), \sin(\delta_b))$  in the direction of the starting point  $B'$ , and  $\overrightarrow{OS}$  has coordinates

$$(R_S \cos(\phi) \cos(\theta), R_S \cos(\phi) \sin(\theta), R_S \sin(\phi)),$$

with  $R_S = R + h$  is the geocentric radius  $R$  plus the altitude  $h$  of station  $S$ ,  $\phi$  is the geocentric latitude of  $S$  and  $\theta$  is the local sidereal time in  $S$ . An analogous expression  $\overrightarrow{SF} = \overrightarrow{OS} + \lambda_f v_f$  can be obtained, where  $\lambda_f$  is now the distance between the station  $S$  and  $F$ , and  $v_f$  is an unitary vector in the direction of the ending point  $F'$ .

The vectorial equation

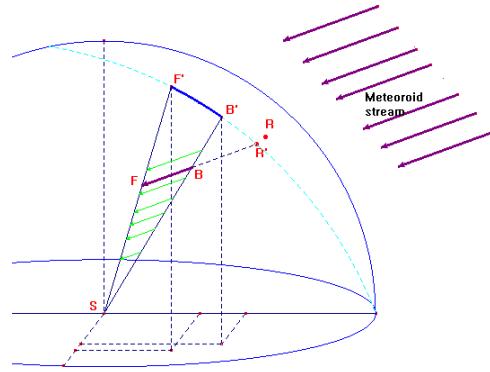
$$\overrightarrow{BF} = \overrightarrow{SF} - \overrightarrow{SB}$$

proposes a system of equations whose solutions  $\lambda_f$  and  $\lambda_b$  give an estimate of the starting and ending

TABLE 1

## RESULTS OBTAINED FROM THE OBSERVATION OF TWO STATIONS

	Starting point	Ending point
Longitude.	4°.178W	4°.258W
Latitude	38°.161N	38°.031N
Altitude	106.7 Km	75.7 Km
Distance	189.7 Km	162.0 Km
Time: 0.59s	Mag.: -4.9	Phot. mass: 3.2g

Fig. 3. In green, possible trajectories directed to  $R'$ . In purple, trajectory coherent with the speed of the stream.

distances and, therefore, of the atmospheric trajectory of the meteoroid. Tables 2 and 3 have been calculated from a single image of the BOOTES-2 station using the typical speed (Madiedo 2017; Rendtel 2017) of the Perseids within a ±3km/s speed interval. The concordance with the results obtained with multiple stations is remarkable. For the calculation of photometric masses, the method described in Ceplecha & McCrosky (1976) and Madiedo (2017) has been followed.

With the previous estimate of the distances, a second check can be made between the estimated angular velocities and the typical one for shower to confirm the association of the meteoroid with the active showers.

## 3. ONLY SINGLE STATION AND UNKNOWN TIME

In this case, for each possible initial altitude  $h_i$  there exists a unique vector  $\overrightarrow{BF}$  with origin in the line  $\overline{SB'}$  at altitude  $h_i$ , end in the line  $\overline{SF'}$ , whose direction is the opposite of the apparent radiant  $R'$  (see Figure 4). Using the same notation that the above section, we now propose the second degree equation in  $\lambda_b$ :

$$\|\overrightarrow{OS} + \lambda_b v_b\| = R + h_i,$$

TABLE 2

ESTIMATED ATMOSPHERIC TRAJECTORIES  
WITH DATA OF A SINGLE STATION FOR A  
RANGE OF SPEEDS (KNOWN TIME)

Vel.	Long.	Lat.	Alt.(Km)	Dist.(Km)
Beginning				
56 Km/s	4°.179W	38°.062N	99.6	176.9
59 Km/s	4°.186W	38°.131N	105.1	186.4
62 Km/s	4°.193W	38°.200N	110.5	195.9
End				
56 Km/s	4°.267W	37°.961N	73.1	154.1
59 Km/s	4°.280W	38°.038N	77.1	162.3
62 Km/s	4°.292W	38°.106N	81.1	170.5

TABLE 3

MAGNITUDE AND PHOTOMETRIC MASS  
ESTIMATED WITH DATA OF A SINGLE  
STATION FOR A RANGE OF SPEEDS  
(KNOWN TIME)

Velocity	Magnitude	Phot. mass (g)
56 Km/s	-5.0	3.9
59 Km/s	-5.1	4.3
62 Km/s	-5.2	4.8

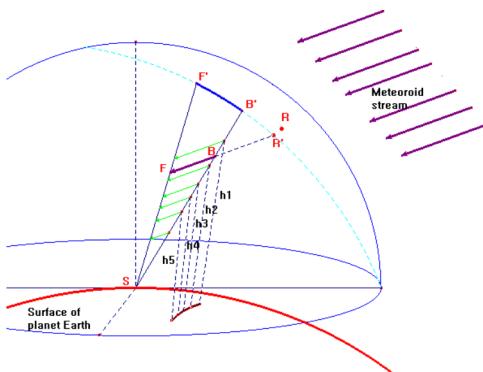


Fig. 4. Each possible trajectory (in green) starts at a different altitude. Some of them (in purple) will be within a reasonable range of altitudes.

This equation can have two solutions, one in the direction  $\vec{SB}$ , and another in the opposite direction. The choice is obvious. Abnormal results are indicators that the association to a shower is not correct.

Tables 4 and 5 show the results obtained for a range of initial heights between 120 and 90 kilometers.

TABLE 4

ESTIMATED ATMOSPHERIC TRAJECTORIES  
WITH DATA OF A SINGLE STATION FOR A  
RANGE OF ALTITUDES (UNKNOWN TIME)

Alt.	Long.	Lat.	Dist.(Km)
Beginning			
120.0 Km	4°.206W	38°.320N	212.6
112.5 Km	4°.196W	38°.226N	199.5
105.0 Km	4°.186W	38°.131N	186.5
97.5 Km	4°.176W	38°.036N	173.4
90.0 Km	4°.166W	37°.941N	160.2
End			
88.2 Km	4°.313W	38°.200N	185.1
82.6 Km	4°.297W	38°.112N	173.7
77.1 Km	4°.280W	38°.025N	163.4
71.6 Km	4°.263W	37°.937N	151.0
66.1 Km	4°.246W	37°.849N	139.5

TABLE 5

ESTIMATED MAGNITUDE AND  
PHOTOMETRIC MASS WITH DATA OF A  
SINGLE STATION FOR A RANGE OF  
ALTITUDES (UNKNOWN TIME)

Altitude	Magnitude	Phot. mass (g)
120 Km	-5.3	7.7
105 Km	-5.1	4.3
90 Km	-5.0	3.1

The above results have been calculated from a single image obtained at the BOOTES-2 station for some initial altitudes. So, even using only one station and without precise timing information, a range of magnitudes and masses can be estimated.

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